

1-1. Let $Q > P$.

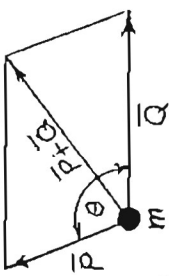
$$a_{\max} = \frac{1}{m}(Q+P), \quad a_{\min} = \frac{1}{m}(Q-P)$$

$$\frac{a_{\max}}{a_{\min}} = \frac{Q+P}{Q-P} = 3, \text{ giving } Q = 2P.$$

Mean acceleration = $\frac{1}{2}(a_{\max} + a_{\min}) = \frac{Q}{m} = \frac{1}{m}|\vec{P} + \vec{Q}|$

Hence $Q = |\vec{P} + \vec{Q}|$. By cosine law, $|\vec{P} + \vec{Q}|^2 = Q^2 + P^2 + 2QP \cos \theta = Q^2$

Then $P^2 = -2QP \cos \theta = -4P^2 \cos \theta$ or $\cos \theta = -1/4$, $\theta = 104.48^\circ$



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1-2. (a) Auto position $\vec{r}_a = 30t \vec{i}$ meters

Plane position $\vec{r}_p = 1000 \vec{i} + 90t \vec{j} + 1000 \vec{k}$ meters

Relative position $\vec{r}_{p/a} = \vec{r}_p - \vec{r}_a = (1000 - 30t) \vec{i} + 90t \vec{j} + 1000 \vec{k}$

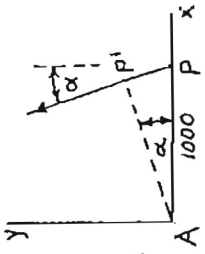
Relative velocity $\vec{v}_{p/a} = \frac{d}{dt}(\vec{r}_{p/a}) = -30 \vec{i} + 90 \vec{j}$ m/sec

(b) $AP' = 1000 \cos \alpha$, $\alpha = \tan^{-1} \frac{1}{3}$

$$\text{or } AP' = 1000 \frac{3}{\sqrt{10}}$$

Separation $d_{\min} = \sqrt{(AP')^2 + 1000^2}$

$$= 1000 \sqrt{\frac{9}{10} + 1} = 1378.4 \text{ meters}$$



1-3. Given $\vec{e}_1 = l_1 \vec{i} + l_2 \vec{j} + l_3 \vec{k}$

$$\vec{e}_2 = m_1 \vec{i} + m_2 \vec{j} + m_3 \vec{k}$$

$$\vec{e}_3 = n_1 \vec{i} + n_2 \vec{j} + n_3 \vec{k}$$

$$(b) \vec{e}_1 \cdot (\vec{e}_2 \times \vec{e}_3) = \begin{vmatrix} l_1 & l_2 & l_3 \\ m_1 & m_2 & m_3 \\ n_1 & n_2 & n_3 \end{vmatrix} = 0$$

(c) Equations of part (a)
and
 $l_1 m_1 + l_2 m_2 + l_3 m_3 = 0$
 $l_1 n_1 + l_2 n_2 + l_3 n_3 = 0$
 $m_1 n_1 + m_2 n_2 + m_3 n_3 = 0$

$$4. \bar{A} = A_x \bar{i} + A_y \bar{j} + A_z \bar{k}$$

$$= A_1 \bar{e}_1 + A_2 \bar{e}_2 + A_3 \bar{e}_3$$

where

$$\begin{cases} \bar{e}_1 = \bar{i} \\ \bar{e}_2 = \frac{1}{\sqrt{2}}(\bar{i} + \bar{j}) \\ \bar{e}_3 = \frac{1}{\sqrt{2}}(\bar{i} + \bar{k}) \end{cases}$$

equating \bar{i} components,

$$A_1 + \frac{A_2}{\sqrt{2}} + \frac{A_3}{\sqrt{2}} = A_x$$

from \bar{j} components, $\frac{A_2}{\sqrt{2}} = A_y$

from \bar{k} components, $\frac{A_3}{\sqrt{2}} = A_z$

$$A_1 = A_x - A_y - A_z$$

$$A_2 = \sqrt{2} A_y$$

$$A_3 = \sqrt{2} A_z$$

5. Given $[L], [M], [F]$ are fundamental.

$= ma$, so the dimensions of acceleration $[A] = [M^{-1} F]$

$$[A] = [L T^{-2}] \text{ or } [T] = \left[\frac{L}{A} \right] = \left[\frac{L}{M^{-1} F} \right]$$

6. Fundamental units: mass — kg

length — cm

time — sec

Density of water $\rho = 1 \text{ g/cm}^3 = 1000 \text{ kg/m}^3$

Specific wt. $w = \rho g = 9810 \frac{\text{kg}}{\text{m}^3 \text{sec}^2} = 1 \frac{\text{kg}}{\text{cm}^3 \text{sec}^2}$

$$\text{Hence } l = 9810 \left(\frac{\text{cm}}{\text{m}} \right)^2 \left(\frac{\text{sec}}{\text{sec}} \right)^2 = 9810 \text{ a}^2 \text{ b}^2$$

$$\text{Accel. of gravity} = 9.81 \frac{\text{m}}{\text{sec}^2} = 1 \frac{\text{cm}}{\text{sec}^2} \text{ or } 9.81 = \frac{a}{b^2}$$

Multiply equations. $9.81 = 9810 \text{ a}^3$ giving $a = 0.1$

$$\text{Then } b = \sqrt{\frac{a}{9.81}} = \frac{1}{\sqrt{98.1}} = 0.1010$$

$$1 \text{ cm} = 0.1000 \text{ meters}$$

$$1 \text{ sec} = 0.1010 \text{ sec}$$

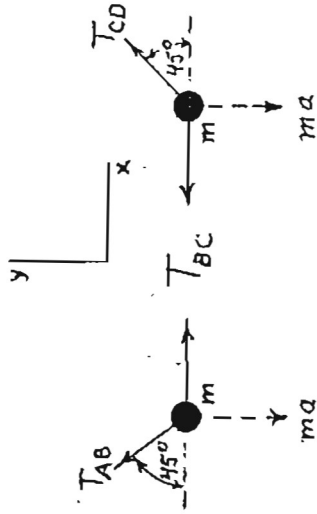
1-7.

$$a = \sqrt{19^2 + 9.5^2} = 21.243 \frac{\text{m}}{\text{sec}^2}$$

For $v = 3000 \text{ m/sec}$,

$$\omega v = 9.5 \frac{\text{m}}{\text{sec}^2}, \quad \omega = \frac{9.5}{3000} = 3.167 \times 10^{-3} \frac{\text{rad}}{\text{sec}}$$

1-8. Use d'Alembert's principle.



Sum y forces on system. $\frac{1}{\sqrt{2}}(T_{AB} + T_{CD}) = 2ma$

Sum x forces on each particle, $T_{BC} = \frac{T_{AB}}{\sqrt{2}} = \frac{T_{CD}}{\sqrt{2}}$

Then $T_{AB} = T_{CD} = \sqrt{2} ma, \quad T_{BC} = ma$

2-1. $\omega = \alpha t$ where $\alpha = \text{const.}$
 Integrate to obtain $\theta = \frac{1}{2} \alpha t^2$
 Acceleration of P is

$$\vec{a} = \vec{a}_0 + \vec{a}_p$$

where the horizontal acceleration $\vec{a}_0 = r\alpha(\sin\theta\vec{e}_r + \cos\theta\vec{e}_\theta)$
 P moves in a circular path relative to O.

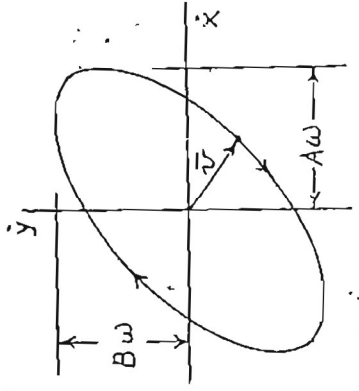
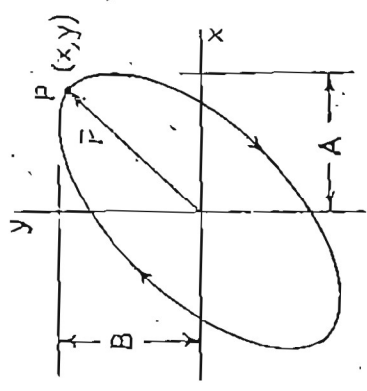
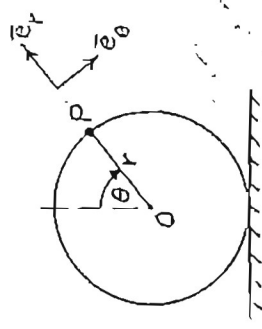
$$\vec{a}_{p/O} = -r(\alpha t)^2\vec{e}_r + r\alpha\vec{e}_\theta$$

$$\vec{a} = r\alpha[(\sin\theta - \alpha t^2)\vec{e}_r + (1 + \cos\theta)\vec{e}_\theta]$$

Hence.

2-2. Given $x = A \cos \omega t$
 $y = B \cos(\omega t + \beta)$
 Then $\dot{x} = -A\omega \sin \omega t$
 $\dot{y} = -B\omega \sin(\omega t + \beta)$

The hodograph is a plot of $\vec{v} = \dot{x}\vec{i} + \dot{y}\vec{j}$
 Note that the two ellipses have the same shape.

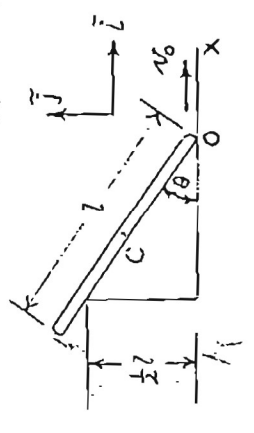


2-3. Speed $s = v_0$ and $s = \omega \rho$
 $\vec{a} = \dot{s}\vec{e}_t + \frac{s^2}{\rho}\vec{e}_n$

From Eq. (2-61), $\rho = R(1+k^2)$
 $= R(1+(\tan^2 30^\circ)) = \frac{4}{3}R$

Then we obtain $\vec{a} = a_0\vec{e}_t + \frac{3v_0^2}{4R}\vec{e}_n$

2nd method: Use the horizontal component of velocity and a circular path of radius R to obtain $a_n = \frac{(v_0 \cos 30^\circ)^2}{R} = \frac{3v_0^2}{4R}$



2-4. Position x of lower end O is $x = \frac{1}{2}l \cot \theta$
 giving $\dot{x} = -\frac{1}{2}l\theta \csc^2 \theta = -v_0$
 or $\dot{\theta} = -\frac{2v_0}{l} \sin^2 \theta$

(b) Differentiate again. $\ddot{\theta} = \frac{-4v_0\dot{\theta}}{l} \sin \theta \cos \theta$
 Using $\dot{\theta}$ expression, $\ddot{\theta} = \frac{8v_0^2}{l^2} \sin^3 \theta \cos \theta$

(c) $\vec{v}_C = \vec{v}_O + \vec{v}_{C/O} = v_0\vec{i} + \frac{1}{2}l\dot{\theta}(\sin\theta\vec{i} + \cos\theta\vec{j})$
 $= v_0\vec{i} + \frac{1}{2}l\left(\frac{-2v_0}{l}\sin^3\theta\right)(\sin\theta\vec{i} + \cos\theta\vec{j})$
 or $\vec{v}_C = v_0[(1 - \sin^3\theta)\vec{i} - \sin^2\theta \cos\theta\vec{j}]$