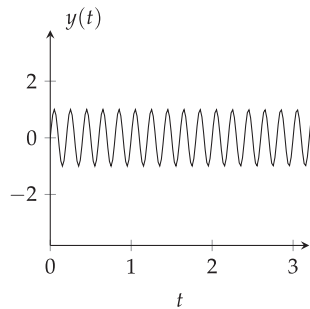


(a) $y(t) = 2 \sin(4\pi f t)$



(b) $y(t) = \sin(10\pi f t)$

Figure 2.1: Plots of $y(t) = A \sin(2\pi f t)$ on $[0, 5]$ for $f = 2$ Hz and $f = 5$ Hz.

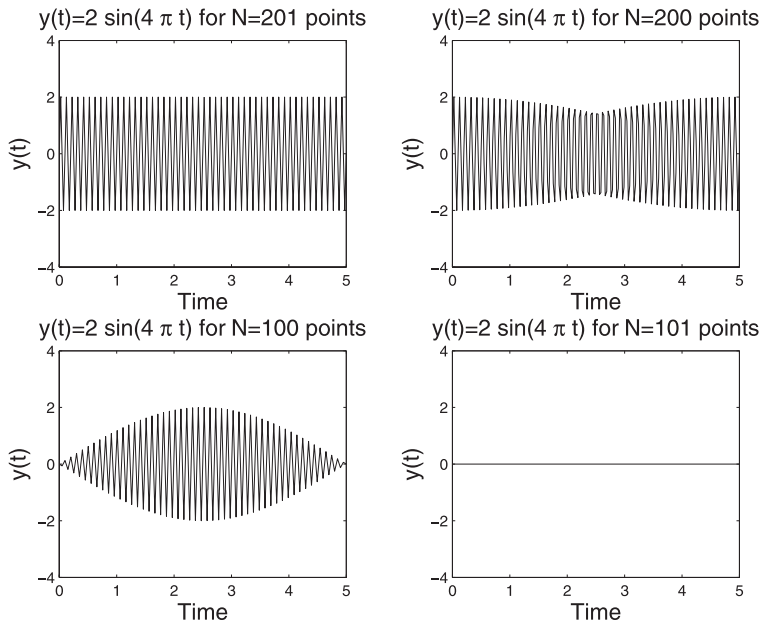
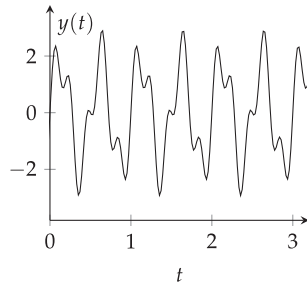
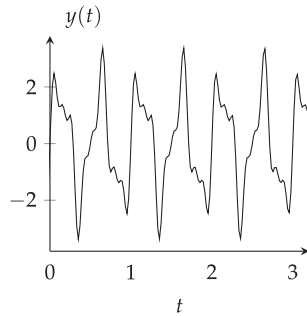


Figure 2.2: Problems can occur while plotting. Here we plot the function $y(t) = 2 \sin 4\pi t$ using $N = 201, 200, 100, 101$ points.

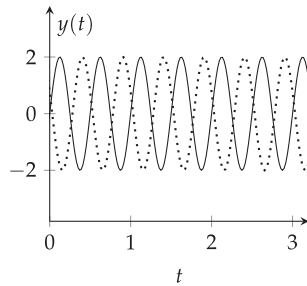


(a) Sum of signals with frequencies
 $f = 2$ Hz and $f = 5$ Hz.

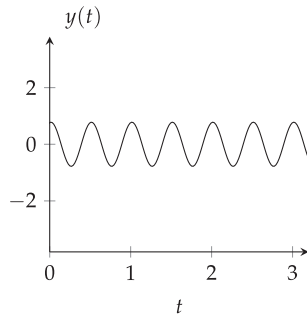


(b) Sum of signals with frequencies
 $f = 2$ Hz, $f = 5$ Hz, and $f = 8$ Hz.

Figure 2.3: Superposition of several sinusoids.

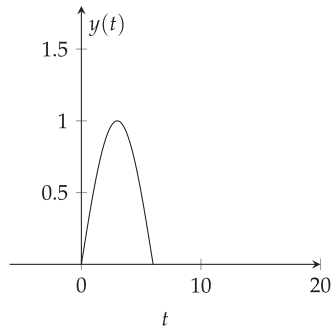


(a) Plot of each function.

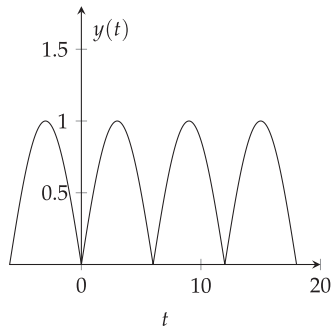


(b) Plot of the sum of the functions.

Figure 2.4: Plot of the functions $y(t) = 2 \sin(4\pi t)$ and $y(t) = 2 \sin(4\pi t + 7\pi/8)$ and their sum.



(a) Plot of function $f(t)$.



(b) Periodic extension of $f(t)$.

Figure 2.5: Plot of the function $f(t)$ defined on $[0, 2\pi]$ and its periodic extension.

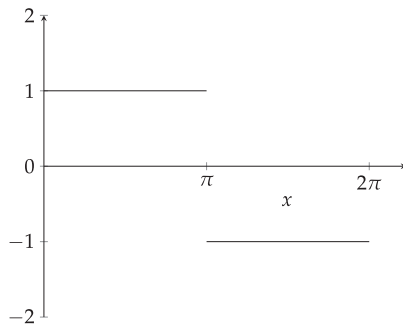


Figure 2.6: Plot of discontinuous function in Example 2.3.

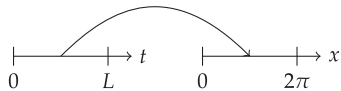


Figure 2.7: A sketch of the transformation between intervals $x \in [0, 2\pi]$ and $t \in [0, L]$.

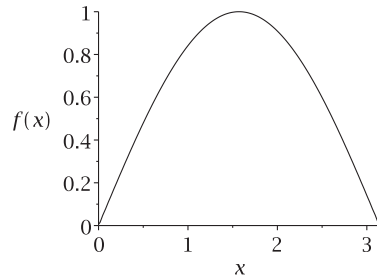


Figure 2.8: Plot of the first fifty terms of the Fourier series representation for $f(x) = \sin x$, $x \in [0, \pi]$.

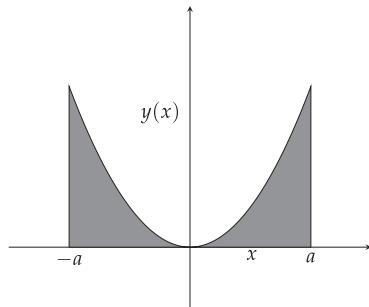


Figure 2.9: Area under an even function on a symmetric interval, $[-a, a]$.

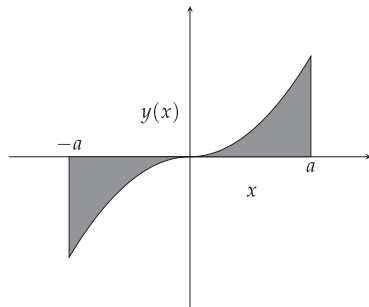


Figure 2.10: Area under an odd function on a symmetric interval, $[-a, a]$.

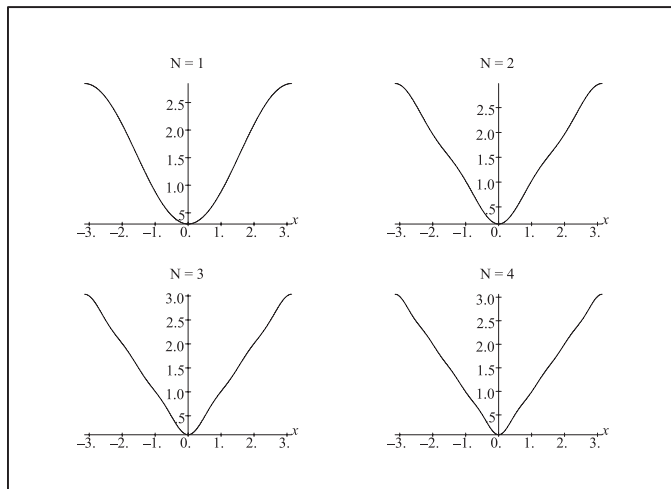


Figure 2.11: Plot of the first partial sums of the Fourier series representation for $f(x) = |x|$ on the interval $x \in [-\pi, \pi]$.

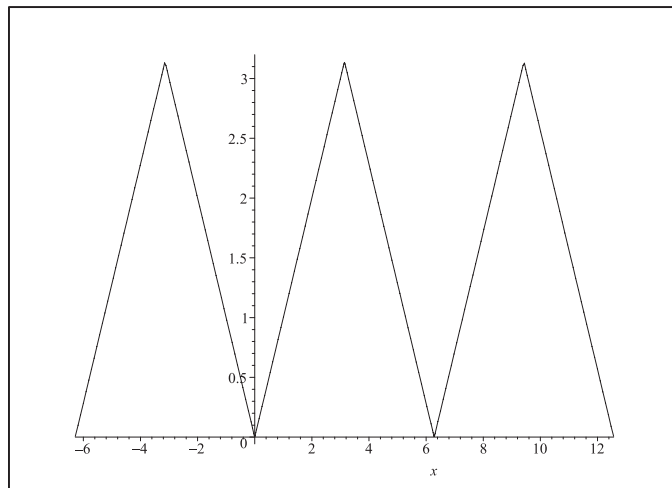


Figure 2.12: Plot of the first 10 terms of the Fourier series representation for $f(x) = |x|$ on the interval $x \in [-2\pi, 4\pi]$.

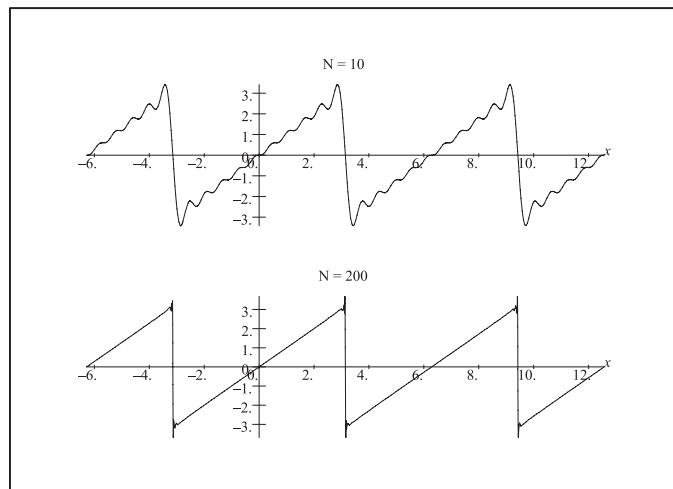


Figure 2.13: Plot of the first 10 terms and 200 terms of the Fourier series representation for $f(x) = x$ on the interval $x \in [-2\pi, 4\pi]$.

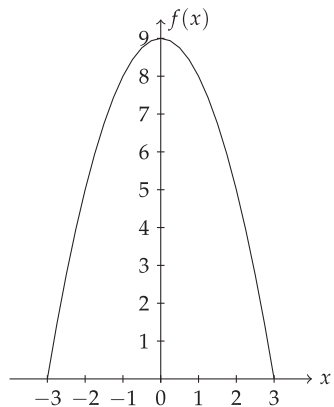


Figure 2.14: Plot of $f(x) = 9 - x^2$ for $x \in [-3, 3]$.

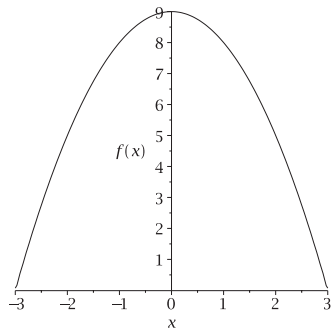


Figure 2.15: Plot of the first fifty terms of the Fourier series representation of $f(x) = 9 - x^2$ for $x \in [-3, 3]$.

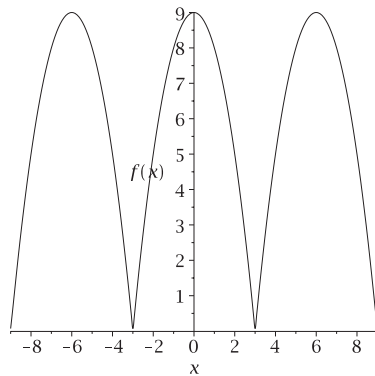


Figure 2.16: Plot of the periodic extension of the Fourier series representation of $f(x) = 9 - x^2$ for $x \in [-3, 3]$.

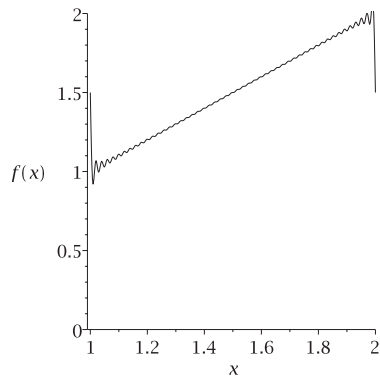


Figure 2.17: Plot of the first fifty terms of the Fourier series representation for $f(x) = x$, $x \in [1, 2]$.

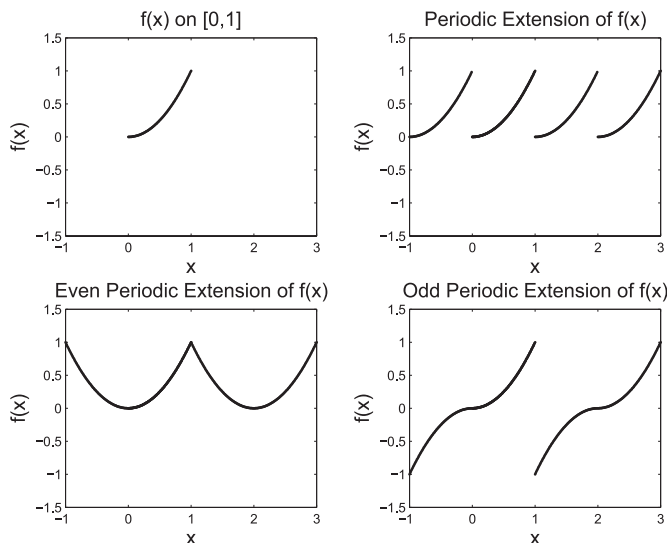


Figure 2.18: This is a sketch of a function and its various extensions. The original function $f(x)$ is defined on $[0, 1]$ and graphed in the upper left corner. To its right is the periodic extension, obtained by adding replicas. The two lower plots are obtained by first making the original function even or odd and then creating the periodic extensions of the new function.

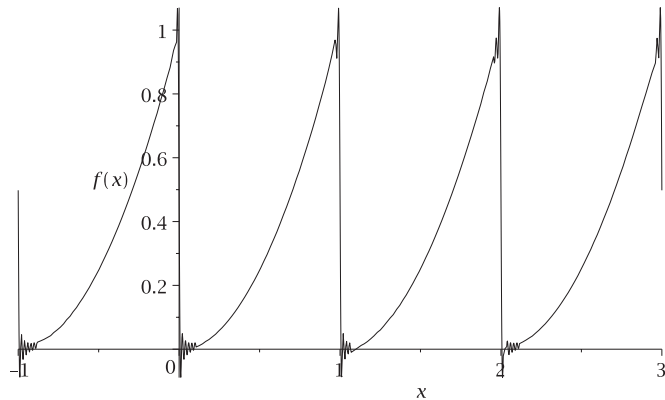


Figure 2.19: The periodic extension of $f(x) = x^2$ on $[0, 1]$.

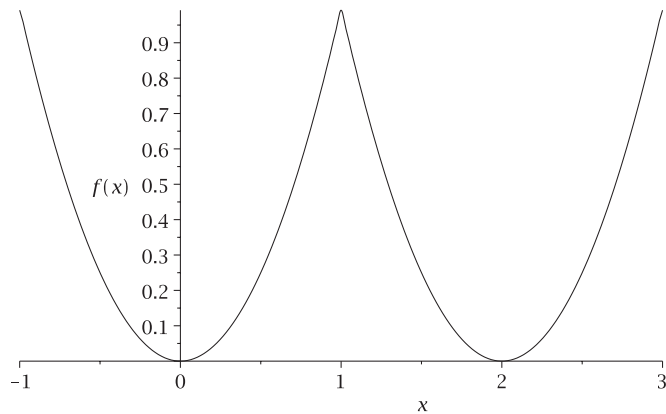


Figure 2.20: The even periodic extension of $f(x) = x^2$ on $[0, 1]$.

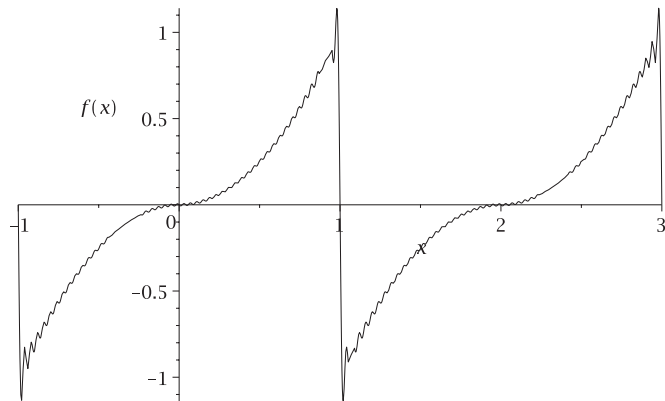


Figure 2.21: The odd periodic extension of $f(x) = x^2$ on $[0, 1]$.

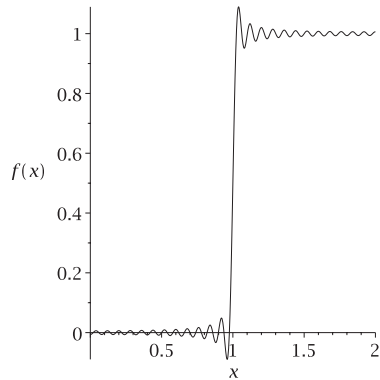


Figure 2.22: Plot of the first fifty terms of the Fourier Cosine Series representation for Example 2.14.

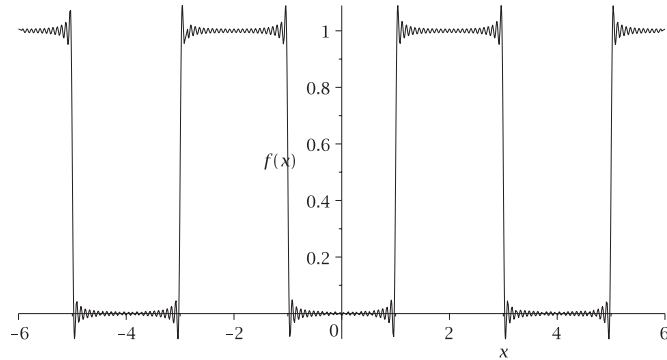


Figure 2.23: Plot of the first fifty terms of the Fourier Cosine Series representation for Example 2.14 for $x \in [-6, 6]$.

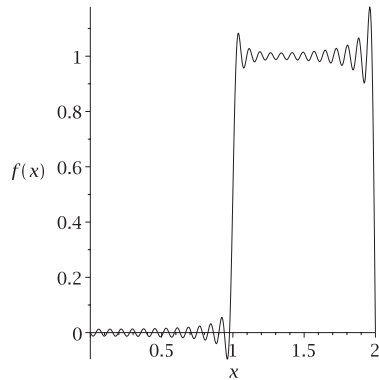


Figure 2.24: Plot of the first fifty terms of the Fourier Sine Series representation for Example 2.15.

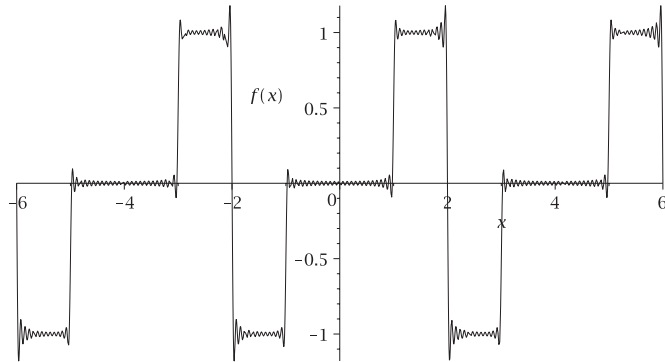


Figure 2.25: Plot of the first fifty terms of the Fourier Sine Series representation for Example 2.15 for $x \in [-6, 6]$.

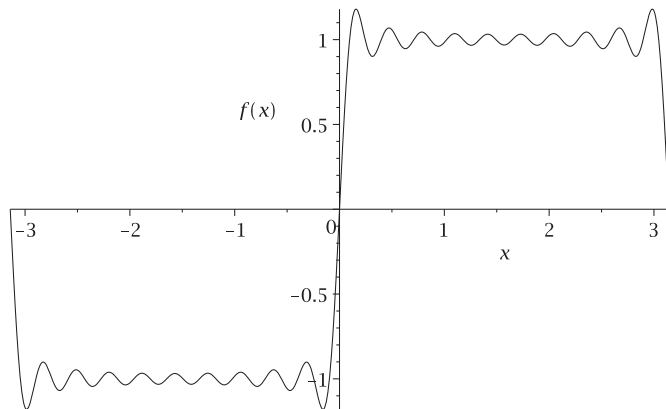


Figure 2.26: The Fourier series representation of a step function on $[\pi, \pi]$ for $N = 10$.

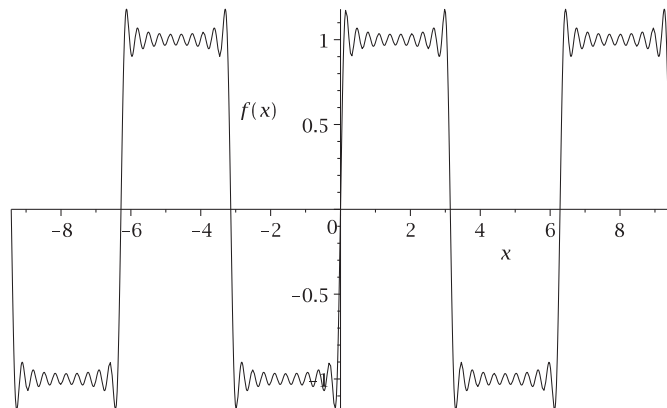


Figure 2.27: The Fourier series representation of a step function on $[-\pi, \pi]$ for $N = 10$ plotted on $[-3\pi, 3\pi]$ displaying the periodicity.

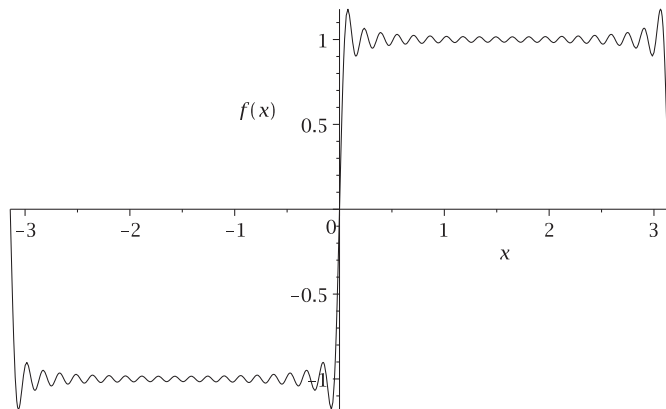


Figure 2.28: The Fourier series representation of a step function on $[-\pi, \pi]$ for $N = 20$.

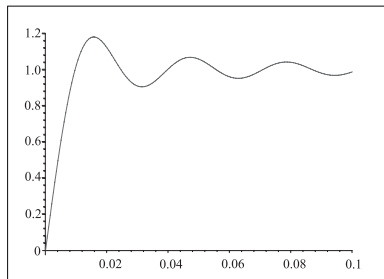


Figure 2.29: The Fourier series representation of a step function on $[-\pi, \pi]$ for $N = 100$.

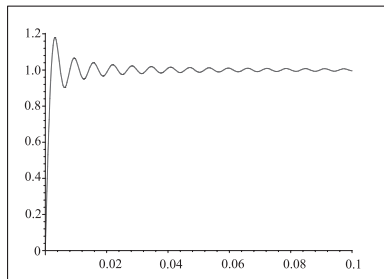


Figure 2.30: The Fourier series representation of a step function on $[-\pi, \pi]$ for $N = 500$.

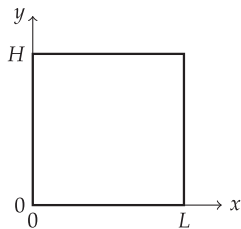


Figure 2.31: The rectangular membrane of length L and width H . There are fixed boundary conditions along the edges.

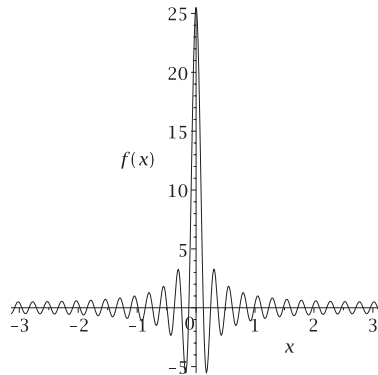


Figure 2.32: N th Dirichlet Kernel for $N=25$.

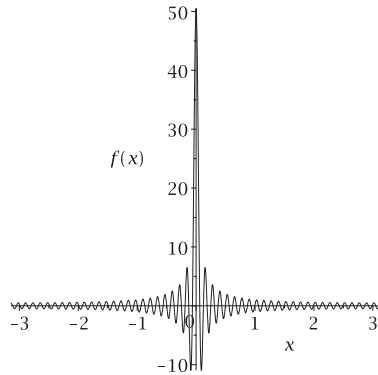


Figure 2.33: N th Dirichlet Kernel for $N=50$.

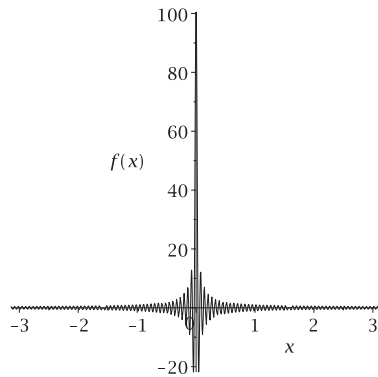


Figure 2.34: N th Dirichlet Kernel for $N=100$.

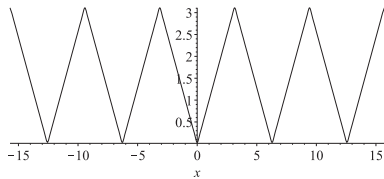


Figure 2.35: N th Partial Sum in Maple.

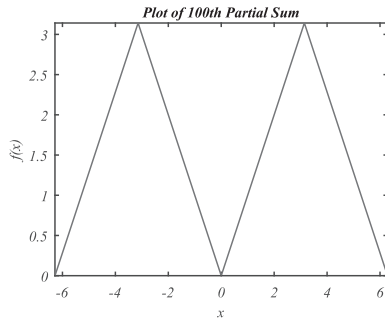


Figure 2.36: N th Partial Sum done in MATLAB.

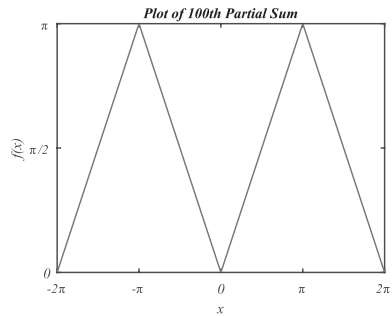


Figure 2.37: N th Partial Sum.

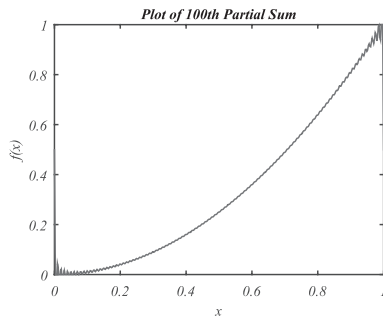


Figure 2.38: N th Partial Sum for $f(x) = x^2$ on $x \in [0,1]$ as found in MATLAB using symbolic computation of the Fourier coefficients.