

Chapter 2

Problem 2

We have $g_1(t) = g(\alpha t)$, where $\alpha > 1$

Let $u = \alpha t$. This implies that $t = u / \alpha$ where α is the scaling factor with $\alpha > 1$

Then

$$FT\{g_1(t)\} = FT\{g(\alpha t)\} = \int_{-\infty}^{\infty} g(\alpha t) e^{-jft} dt = \int_{-\infty}^{\infty} g(u) e^{-jfu/\alpha} d(u/\alpha) = \frac{1}{\alpha} G\left(\frac{f}{\alpha}\right)$$

Problem 4

$$\begin{aligned} FT\{g_1(t) * g_2(t)\} &= \int \left[\int x(\tau) y(t - \tau) d\tau \right] e^{-jft} dt \\ &= \int x(\tau) \left[\int y(t - \tau) e^{-jft} dt \right] d\tau \\ &= \int x(\tau) e^{-u\tau} \left[\int y(t - \tau) e^{-v(t - \tau)} d(t - \tau) \right] d\tau \\ &= G_1(u) \cdot G_2(v) \end{aligned}$$

Problem 6

As $F(u) = g(t)$, we have

$$g(t) = F^{-1}\{G(u)\} = \frac{1}{2\pi} \int G(u) e^{jft} df$$

Let $t' = -t$, we get

$$g(-t') = \frac{1}{2\pi} \int G(jf) e^{-jft'} df$$

Interchanging t' and f we get

$$2\pi g(-f) = \int G(t') e^{-jft'} dt' = F\{G(t)\}$$

$$g(-f) = \int G(t') e^{-j2\pi ft'} dt' = F\{G(t)\}$$

Problem 8:

Use the same code for problem 1-2 d to find the fft of the signal

Problem 10:

```
Order=9;  
Wn=[200]/(samplerate/2);  
[b1,a1]=butter(n,Wn);  
FilteredSig=filter(b1,a1,SIG);
```

Chapter 3

Problem 2

```
I=imread('p_3_2.jpg');
I=rgb2gray(I);
figure;imshow(I);
S=size(I);
I=double(I);
I=dec2base(I,2);
newS=size(I)
J=zeros(S(1),S(2));
for i=1:newS(1)
    k=char(I(i,:));
    k(1) = '0';
    k(2) = '0';
    k(3) = '0';
    // k(4) = '0'; //Uncomment this line to solve section b
    k=base2dec(k,2);
    a=fix(i/S(1))+1;
    b=mod(i,S(1));
    if b == 0
        b=S(1);
        a=a-1;
    end
    J(b,a)=k;
end
figure;imshow(J,[0 255]);
```

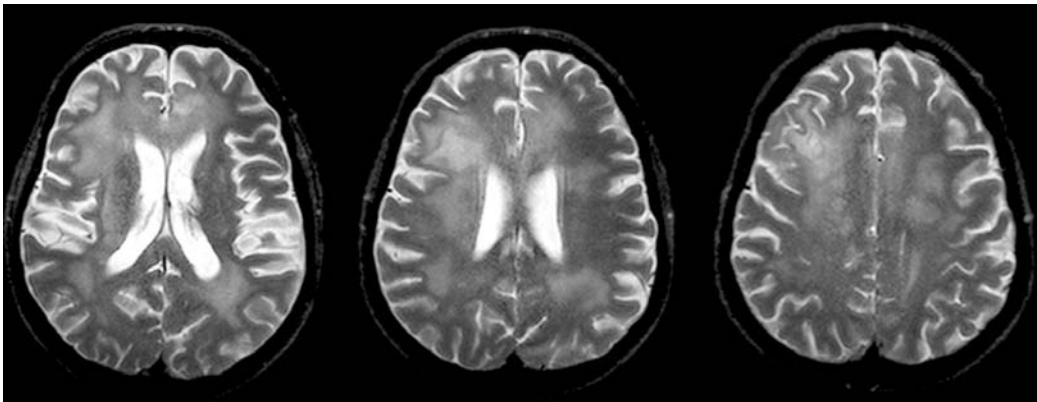


Image before elimination of any bit(file: p_3_2.jpg)