

Chapter 2

Properties of Engineering Materials

1- What is the stress in a wire whose diameter is 1 mm, which supports a load of 100 Newton

Solution:

$$\sigma = \frac{\text{load}}{\text{area}} = \frac{100}{\frac{\pi \left(\frac{1}{1000}\right)^2}{4}} = \frac{400}{\pi} (1000)^2 = 127 \text{ MPa}$$
$$= 127 \text{ N/mm}^2$$

2- Suppose that the wire in the above problem is copper and is 30 m long. How much will it stretch? Repeat for a steel and aluminum wires

Solution:

Cu wire:

$$\varepsilon = \frac{\sigma}{E} = \frac{127000000}{10 \times 10^{10}}$$

Total elongation for copper wire (Δl_{cu})

Since $\varepsilon = \frac{\Delta l}{l}$

$$\Delta l_{\text{cu}} = \varepsilon l = \frac{127000000}{10 \times 10^{10}} \times 30 = 0.038 \text{ m} = 38 \text{ mm}$$

Steel wire:

$$\varepsilon = \frac{\sigma}{E} = \frac{127000000}{21 \times 10^{10}}$$

Total elongation for copper wire (Δl_{st})

Since $\varepsilon = \frac{\Delta l}{l}$

$$\Delta l_{\text{st}} = \varepsilon l = \frac{127000000}{21 \times 10^{10}} \times 30 = 0.018 \text{ m} = 18 \text{ mm}$$

Aluminum wire:

$$\varepsilon = \frac{\sigma}{E} = \frac{127000000}{7 \times 10^{10}}$$

Total elongation for copper wire (Δl_{al})

Since $\varepsilon = \frac{\Delta l}{l}$

$$\Delta l_{al} = \varepsilon \times l = \frac{127000000}{7 \times 10^{10}} \times 30 = 0.054 \text{ m} = 54 \text{ mm}$$

Comment: Steel is stiffer than both copper and aluminum. It is exactly 3 times more stiff than aluminum

3- Estimate the HB hardness of an alloy steel of ultimate tensile strength TS=1500 MPa using equation 2.9. Use the hardness conversion table to determine the HRC hardness.

Solution:

$$TS \text{ (MPa)} = 3.5 \text{ HB}$$

$$HB = \frac{1500}{3.5} = 428$$

Using the conversion table 2.3, the corresponding HRC of that alloy steel = 46
Referring to Figure 2.5 the hardness values are realized.

4- A constructional component made of Al-alloy can be represented as a bar of diameter 20 mm and length 400 mm is subjected to pure tension; calculate:
a- Extension of the bar if the imposed load= 8 kN
b-The load at which the bar suffers permanent deformation
c- Maximum load the bar can withstand fracture

Assume the following mechanical properties: E=70 GPa, YS=496 MPa, TS=560 MPa

Solution:

a- $A_o = \frac{\pi \times 20^2}{4} = 314 \text{ mm}^2$

$$\begin{aligned} \text{Imposed tensile strength} &= \frac{8000}{314} = 255 \text{ N/mm}^2 \\ &= 255 \text{ MPa} \end{aligned}$$

It is thus less than the YS, which means that the deformation will be purely elastic.

b- $YS = \sigma_{0.2} = 496 \text{ N/mm}^2$
 $F_y = \sigma_{0.2} \times A_o = 496 \times 314 = 156 \text{ kN}$

c- $F_{max} = TS \times A_o = 560 \times 314 = 176 \text{ kN}$