

"Problem 2.9"

$$P_{\infty}=101330.$$

$$T_{\infty}=300.$$

$$T_s=325.$$

$$U_{\infty}=2.1$$

$$x_1=0.42$$

$$x_2=1.5$$

$$q_{dd,1}=107.$$

$$q_{dd,2}=57$$

$$M_{air}=29$$

$$M_{H_2O}=18$$

"Properties"

$$T_{film}=0.5*(T_s+T_{\infty})$$

$$\rho=\text{density}(\text{air}, P=P_{\infty}, T=T_{film})$$

$$C_P=CP(\text{air}, T=T_{film})$$

$$k=\text{conductivity}(\text{air}, T=T_{film})$$

$$\mu=\text{viscosity}(\text{air}, T=T_{film})$$

$$Pr=\text{Prandtl}(\text{air}, T=T_{film})$$

"Find Re_x at the two locations"

$$Re_{x1}=\rho*U_{\infty}*x_1/\mu$$

$$Re_{x2}=\rho*U_{\infty}*x_2/\mu$$

"At both locations we deal with laminar regime. Therefore assume $Nu_x=cRe_x^nPr^{1/3}$ nad calculate c and n"

$$h_{x1}*x_1/k=C*Re_{x1}^n*Pr^{1/3}$$

$$h_{x2}*x_2/k=C*Re_{x2}^n*Pr^{1/3}$$

$$q_{dd,1}=h_{x1}*(T_s-T_{\infty})$$

$$q_{dd,2}=h_{x2}*(T_s-T_{\infty})$$

"Knowing n, we can find the mas fluxes by using analogy between heat and mass transfer"

"From Table in Appendix H"

$$D_{12}=(0.26e-4)*(T_{\infty}/298)^{3/2}$$

$$Sc=(\mu/\rho)/D_{12}$$

$$P_s=P_{sat}(\text{water}, T=T_{\infty})$$

"Find mass fraction of water vapor at s surface"

$$X_s=P_s/P_{\infty}$$

$$m_{1s}=X_s*M_{H_2O}/(X_s*M_{H_2O}+(1.-X_s)*M_{air})$$

$$K_{x1}*x_1/(\rho*D_{12})=C*Re_{x1}^n*Sc^{1/3}$$

$$m_{dd,x1}=K_{x1}*(m_{1s}-0.0)$$

$$K_{x2}*x_2/(\rho*D_{12})=C*Re_{x2}^n*Sc^{1/3}$$

$$m_{dd,x2}=K_{x2}*(m_{1s}-0.0)$$

"Mass flux is small enough to justify the application of low mass transfer method."

Problem 2.9

$$P_{\infty} = 101330$$

$$T_{\infty} = 300$$

$$T_s = 325$$

$$U_{\infty} = 2.1$$

$$x_1 = 0.42$$

$$x_2 = 1.5$$

$$q_{dd,1} = 107$$

$$q_{dd,2} = 57$$

$$M_{\text{air}} = 29$$

$$M_{\text{H}_2\text{O}} = 18$$

Properties

$$T_{\text{film}} = 0.5 \cdot [T_s + T_{\infty}]$$

$$\rho = \rho [\text{'Air'}, P = P_{\infty}, T = T_{\text{film}}]$$

$$C_P = C_p [\text{'Air'}, T = T_{\text{film}}]$$

$$k = k [\text{'Air'}, T = T_{\text{film}}]$$

$$\mu = \text{Visc} [\text{'Air'}, T = T_{\text{film}}]$$

$$\text{Pr} = \text{Pr} [\text{'Air'}, T = T_{\text{film}}]$$

Find Re_x at the two locations

$$Re_{x1} = \rho \cdot U_{\infty} \cdot \frac{x_1}{\mu}$$

$$Re_{x2} = \rho \cdot U_{\infty} \cdot \frac{x_2}{\mu}$$

At both locations we deal with laminar regime. Therefore assume $Nu_x = c Re_x^n Pr^{(1/3)}$ and calculate c and n

$$h_{x1} \cdot \frac{x_1}{k} = C \cdot Re_{x1}^n \cdot Pr^{[1/3]}$$

$$h_{x2} \cdot \frac{x_2}{k} = C \cdot Re_{x2}^n \cdot Pr^{[1/3]}$$

$$q_{\text{dd},1} = h_{x1} \cdot [T_s - T_{\infty}]$$

$$q_{\text{dd},2} = h_{x2} \cdot [T_s - T_{\infty}]$$

Knowing n , we can find the mass fluxes by using analogy between heat and mass transfer

From Table in Appendix H

$$D_{12} = 0.000026 \cdot \left[\frac{T_{\infty}}{298} \right]^{[3/2]}$$

$$Sc = \frac{\mu}{\rho \cdot D_{12}}$$

$$P_s = P_{\text{sat}} [\text{'Water'}, T = T_{\infty}]$$

Find mass fraction of water vapor at s surface

$$X_s = \frac{P_s}{P_{\infty}}$$

$$m_{1s} = X_s \cdot \left[\frac{M_{H_2O}}{X_s \cdot M_{H_2O} + (1 - X_s) \cdot M_{air}} \right]$$

$$K_{x1} \cdot \frac{x_1}{\rho \cdot D_{12}} = C \cdot Re_{x1}^n \cdot Sc^{[1/3]}$$

$$m_{dd,x1} = K_{x1} \cdot [m_{1s} - 0]$$

$$K_{x2} \cdot \frac{x_2}{\rho \cdot D_{12}} = C \cdot Re_{x2}^n \cdot Sc^{[1/3]}$$

$$m_{dd,x2} = K_{x2} \cdot [m_{1s} - 0]$$

Mass flux is small enough to justify the application of low mass transfer method.

SOLUTION

Unit Settings: SI K Pa J mass deg

$$C = 0.3118$$

$$h_{x1} = 4.28$$

$$K_{x1} = 0.004598$$

$$m_{1s} = 0.02195$$

$$m_{dd,x2} = 0.00005376$$

$$Pr = 0.7246$$

$$q_{dd,1} = 107$$

$$Re_{x2} = 185811$$

$$T_{film} = 312.5$$

$$U_{\infty} = 2.1$$

$$X_s = 0.03489$$

$$C_P = 1005$$

$$h_{x2} = 2.28$$

$$K_{x2} = 0.002449$$

$$M_{air} = 29$$

$$M_{H_2O} = 18$$

$$P_{\infty} = 101330$$

$$q_{dd,2} = 57$$

$$\rho = 1.13$$

$$T_{\infty} = 300$$

$$x_1 = 0.42$$

$$D_{12} = 0.00002626$$

$$k = 0.02657$$

$$\mu = 0.00001915$$

$$m_{dd,x1} = 0.0001009$$

$$n = 0.5053$$

$$P_s = 3536$$

$$Re_{x1} = 52027$$

$$Sc = 0.6455$$

$$T_s = 325$$

$$x_2 = 1.5$$

5 potential unit problems were detected.