

{Example 2.5}

{Based on assumptions, $T_s=25$ C, and concentration of CO₂ at s surface is zero.}

MM_v=18.

MM_air=29.

MM_CO2=44

D_d=0.55e-3

U_d=2.

T_G=25.+273.

T_L=25.+273.

P_G=1.0133e5

phi=0.6

P_sat=P_sat(Water, T=T_G)

P_v=phi*P_sat

X_v=P_v/P_G

m_v=X_v*MM_v/(X_v*MM_v+(1.-X_v)*MM_air)

X_vs=P_sat/P_G

m_vs=X_vs*MM_v/(X_vs*MM_v+(1.-X_vs)*MM_air)

mu_G=viscosity(AIR, T=T_G)

rho_G=density(AIR, T=T_G, P=P_G)

k_G=conductivity(AIR, T=T_G)

nu_G=mu_G/rho_G

C_PG=cp(STEAM, T=T_G, x=1)

D_12=(1.97e-5)*(101330./P_G)*((T_G/256.)^(1.685))

Sc_G=nu_G/D_12

Pr_G=prandtl(AIR, T=T_G)

Sh_G=2.

Sh_G=K_massG*D_d/(rho_G*D_12)

Nus_G=2.

Nus_G=H_G*D_d/k_G

{Part a: First neglect the blowing effect}

m_dd_va1=K_massG*(m_vs-m_v)

{Now include blowing effect}

B_mG=(m_v-m_vs)/(m_vs-1.)

m_dd_va=K_massG*ln(1.+B_mg)

{Part b: Now we have heat transfer as well. However, by fixing T_s at 50 C, evaporation rate will also be fixed, and will be decoupled from HT}

T_sb=273+50

P_vsb=P_sat(water, T=T_sb)

X_vsb=P_vsb/P_G

m_vsb=X_vsb*MM_v/(X_vsb*MM_v+(1.-X_vsb)*MM_air)

B_mGb=(m_v-m_vsb)/(m_vsb-1.)

m_dd_vb=K_massG*ln(1.+B_mgb)

{c: This time we deal with CO₂ mass transfer rate. Let us solve for case (a)}

m_CO2s=0.0

X_CO2G=500.e-6

m_CO2G=X_CO2G*MM_CO2/(X_CO2G*MM_CO2+X_v*MM_v+(1.-X_v-X_CO2G)*MM_air)

D_aCO2=0.16e-4

Sh_G=K_massCO2*D_d/(rho_G*D_aCO2)

{First without the blowing effect:}

m_ddCO2=K_massCO2*(m_CO2s-m_CO2G)

{Now with blowing}

m_ddtot=m_dd_va+m_ddCO2b

B_mGCO2=(m_CO2G-m_CO2s)/(m_CO2s-(m_ddCO2b/m_ddtot))

m_ddCO2b=m_ddtot*m_CO2s+K_massCO2*(ln(1.+B_mGCO2)/B_mGCO2)*(m_CO2s-m_CO2G)

MM_v = 18

MM_air = 29

$$MM_{CO_2} = 44$$

$$D_d = 0.00055$$

$$U_d = 2$$

$$T_G = 25 + 273$$

$$T_L = 25 + 273$$

$$P_G = 101330$$

$$\phi = 0.6$$

$$P_{sat} = P_{sat} \left['Water', T = T_G \right]$$

$$P_v = \phi \cdot P_{sat}$$

$$X_v = \frac{P_v}{P_G}$$

$$m_v = X_v \cdot \left[\frac{MM_v}{X_v \cdot MM_v + (1 - X_v) \cdot MM_{air}} \right]$$

$$X_{vs} = \frac{P_{sat}}{P_G}$$

$$m_{vs} = X_{vs} \cdot \left[\frac{MM_v}{X_{vs} \cdot MM_v + (1 - X_{vs}) \cdot MM_{air}} \right]$$

$$\mu_G = \mathbf{Visc} \left['Air', T = T_G \right]$$

$$\rho_G = \rho \left['Air', T = T_G, P = P_G \right]$$

$$k_G = \mathbf{k} \left['Air', T = T_G \right]$$

$$v_G = \frac{\mu_G}{\rho_G}$$

$$C_{PG} = \mathbf{Cp} \left['Steam', T = T_G, x = 1 \right]$$

$$D_{12} = 0.0000197 \cdot \frac{101330}{P_G} \cdot \left[\frac{T_G}{256} \right]^{1.685}$$

$$Sc_G = \frac{v_G}{D_{12}}$$

$$Pr_G = \mathbf{Pr} \left['Air', T = T_G \right]$$

$$Sh_G = 2$$

$$Sh_G = K_{massG} \cdot \frac{D_d}{\rho_G \cdot D_{12}}$$

$$\text{Nus}_G = 2$$

$$\text{Nus}_G = H_G \cdot \frac{D_d}{k_G}$$

$$m_{dd,va1} = K_{\text{mass}G} \cdot [m_{vs} - m_v]$$

$$B_{mG} = \frac{m_v - m_{vs}}{m_{vs} - 1}$$

$$m_{dd,va} = K_{\text{mass}G} \cdot \ln [1 + B_{mG}]$$

$$T_{sb} = 273 + 50$$

$$P_{vsb} = P_{\text{sat}} [\text{'Water'}, T=T_{sb}]$$

$$X_{vsb} = \frac{P_{vsb}}{P_G}$$

$$m_{vsb} = X_{vsb} \cdot \left[\frac{MM_v}{X_{vsb} \cdot MM_v + (1 - X_{vsb}) \cdot MM_{\text{air}}} \right]$$

$$B_{mGb} = \frac{m_v - m_{vsb}}{m_{vsb} - 1}$$

$$m_{dd,vb} = K_{\text{mass}G} \cdot \ln [1 + B_{mGb}]$$

$$m_{\text{CO}2s} = 0$$

$$X_{\text{CO}2G} = 0.0005$$

$$m_{\text{CO}2G} = X_{\text{CO}2G} \cdot \left[\frac{MM_{\text{CO}2}}{X_{\text{CO}2G} \cdot MM_{\text{CO}2} + X_v \cdot MM_v + (1 - X_v - X_{\text{CO}2G}) \cdot MM_{\text{air}}} \right]$$

$$D_{a\text{CO}2} = 0.000016$$

$$\text{Sh}_G = K_{\text{massCO}2} \cdot \frac{D_d}{\rho_G \cdot D_{a\text{CO}2}}$$

$$m_{dd\text{CO}2} = K_{\text{massCO}2} \cdot [m_{\text{CO}2s} - m_{\text{CO}2G}]$$

$$m_{\text{ddtot}} = m_{dd,va} + m_{dd\text{CO}2b}$$

$$B_{m\text{GCO}2} = \frac{m_{\text{CO}2G} - m_{\text{CO}2s}}{m_{\text{CO}2s} - \frac{m_{dd\text{CO}2b}}{m_{\text{ddtot}}}}$$

$$m_{dd\text{CO}2b} = m_{\text{ddtot}} \cdot m_{\text{CO}2s} + K_{\text{massCO}2} \cdot \frac{\ln [1 + B_{m\text{GCO}2}]}{B_{m\text{GCO}2}} \cdot [m_{\text{CO}2s} - m_{\text{CO}2G}]$$

SOLUTION

Unit Settings: [J]/[K]/[Pa]/[kg]/[degrees]

$$B_{mG} = 0.007998$$

$$B_{mGb} = 0.07276$$

$$B_{m\text{GCO}2} = 0.01198$$

CPG = 1887	D ₁₂ = 0.00002545	DaCO ₂ = 0.000016
D _d = 0.00055	H _G = 92.72	k _G = 0.0255
K _{massCO₂} = 0.06893	K _{massG} = 0.1096	MM _{air} = 29
MM _{CO₂} = 44	MM _v = 18	μ _G = 0.00001848
mCO _{2G} = 0.0007638	mCO _{2s} = 0	m _{ddCO₂} = -0.00005265
m _{ddCO_{2b}} = -0.00005233	m _{ddtot} = 0.000821	m _{dd,va} = 0.0008733
m _{dd,va1} = 0.0008597	m _{dd,vb} = 0.007699	m _v = 0.01163
m _{vs} = 0.01947	m _{vsvb} = 0.07866	Nus _G = 2
v _G = 0.0000156	φ = 0.6	Pr _G = 0.7281
P _G = 101330	P _{sat} = 3141	P _v = 1884
P _{vsvb} = 12253	ρ _G = 1.185	Sc _G = 0.613
Sh _G = 2	T _G = 298	T _L = 298
T _{sb} = 323	U _d = 2	X _{CO_{2G}} = 0.0005
X _v = 0.0186	X _{vs} = 0.031	X _{vsvb} = 0.1209

6 potential unit problems were detected.